## Math 142 <br> Test \#2 Practice Proofs Spring 2022

1. If $m$ is divisible by 4 and $n$ is any even integer, then $m \cdot n$ is divisible by 8 .

Test Hypothesis:
2. If $n^{2}$ is even, then $n$ is even. (HINT: Use an indirect proof).

Test Hypothesis:
3. Prove that if n is odd, the sum of itself and its square is even.

## Test Hypothesis:

4. Prove using an indirect proof, the following:

If $m+n$ is odd, then $m$ or $n$ must be even.

Test Hypothesis:
5. For any integer $n, n-3 n$ is always even. (HINT: Use both cases for $n$, when $n$ is even and when $\mathbf{n}$ is odd).

Test Hypothesis:
6. Prove using induction that $1^{3}+2^{3}+3^{3}+\ldots \ldots .+n^{3}=\left[\frac{n(n+1)}{2}\right]^{2}$

## Test Hypothesis:

Proof by Induction:

